## 3 (Sem-6/CBCS) PHY HE 3

## 2023 PHYSICS

(Honours Elective)

Paper: PHY-HE-6036

## (Advanced Mathematical Physics-II)

Full Marks: 80

Time: Three hours

The figures in the margin indicate full marks for the questions.

1. Answer any ten of the following:

1×10=10

- (a) State Hamilton's Principle.
- (b) Define Generalized co-ordinates.
- (c) What is meant by a Geodesic?

- (d) Generalized coordinates are:
  - (i) Independent
  - (ii) Dependent
  - (iii) Spherical polar coordinates
  - (iv) None of the above
- (e) A particle is moving doing the arc of a circle. The suitable generalized coordinate (s) is/are:
  - (i) ronly
  - (ii)  $\theta$  only
  - (iii) r and  $\theta$  both
  - (iv) x and y
- (f) For a conservative system, the potential energy does not depend upon:
  - (i) force
  - (ii) generalized velocity
  - (iii) generalized coordinator
  - (iv) All of the above

- (g) For a conservative system Hamiltonian represents:
  - (i) T+V
  - (ii) T-V
  - (iii) L + V
  - (iv) 2T V
- (h) If the Lagrangian of a system does not depend on time explicitly, then:
  - (i) the Hamiltonian can not be constant
  - (ii) the Hamiltonian is constant
  - (iii) potential energy is constant
  - (iv) kinetic energy is constant

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- (i) The shortest distance between two points in a plane is:
  - (i) an arc of a circle
  - (ii) an arc of ellipse
  - (iii) a straight line
  - (iv) arbitrary arc

- What is Mutually Exclusive Events?
- (k) Give an example of Collectively Exhaustive events.
- What is Probability Distribution Function?
- (m) What is Compound Probability?
- (n) Define Cyclic group.
- Answer any five of the following:
  - Write Euler Lagrange's differential equations.
  - Explain Principle of List action.
  - What do you mean by canonical coordinates?
  - What do you mean by Lagrangian and Hamiltonian?
  - Define Mathematical Probability and Statistical Probability.
  - Define relation and mapping, (f)

- What are Homomorphism and Isomorphism of group?
- (h) If  $A = \{4, 5\}$  and  $B = \{1, 2, 3\}$  are two sets, then find their Cartesian products A×B and BxA.
- Answer any four of the following: 5×4=20
  - Find the equation of a motion of a simple pendulum using Lagrange's equation.
  - What are Poisson Brackets and Lagrange - Brackets? Prove that both of them do not obey the commutative law of algebra.
  - Define a group and state its postulates. (c)
  - Show that in a group G, identity elements e is unique.
  - Show that a non empty subset H of a (e) group G is a subgroup of G iff
    - (i)  $a, b \in H \Rightarrow ab \in H$ (ii)  $a \notin H \Rightarrow \alpha^{-1} \in H$

- (f) Prove that if P(A) and P(B) are probabilities of two Mutually Exclusive Events A and B then the probability of either of them is P(A or B) = P(A) + P(B).
- 4. Answer any four of the following: 10×4=40
  - (a) Using Euler-Lagrange equation prove that the shortest distance between two fixed points in a plane is a straight line.

    3+7=10
  - (b) Use Hamilton's Principle to find the equation of motion of one dimensional harmonic oscillator. What is modified Hamilton's Principle? 7+3=10
  - (c) Show that a non empty subset H of a group G is a subgroup of G iff
    - (i)  $a, b \in H \Rightarrow ab \in H$
    - (ii)  $a \in H \Rightarrow \alpha^{-1} \in H$  5+5=10
  - (d) Show that under canonical transformation, Poisson-Bracket is invariant.
  - (e) What is the law of Conditional Probabilities? State and prove Bayes' theorem. 4+6=10

(f) What is Random Variable? Explain about probability distribution of a discrete random variable and a continuous random variable.

2+4+4=10

- (g) What is Normal Distribution? Explain with schematic diagrams that how the shape of Normal Distribution curves depends upon the Mean and Standard Deviation. Write importance of Normal Distribution. 2+6+2=10
- (h) Explain the Poisson distribution. Consider an emergency room of a hospital where the past records indicate an average of 5 arrivals daily. The demand for emergency room service at this hospital is distributed according to a Poisson distribution. Calculate the probability of exactly 0, 1, 2, 3, 4 and 5 arrivals. What is the probability of more than 3 arrivals?

  3+5+2=10